

## AMAT100 PRECALCULUS

## EXAM 2A

SPRING 2025

Print Name:

UAlbany Email:

**Directions:** You have **80 minutes** to answer the following questions. ***You must show all necessary work*** as neatly and clearly as possible. Clearly indicate your final answers by placing a box or circle around it.

No calculators, notes, textbooks, mobile phones or other aids are allowed. Do not detach pages.

Problem	Possible	Points
1	9	
2	8	
3	8	
4	6	
5	9	
6	10	
7	6	
8**	4	
Total	56	

\*\*Optional Extra Credit Problem

(Similar to HW5 Questions 2-6)

(1) Let  $L(x)$  be a linear function where  $L(-2) = -3$  and  $L(2) = 3$ .

(a) (3 Points) The slope of the linear function  $L(x)$  is \_\_\_\_\_.

(b) (3 Points) The equation of the linear function is  $L(x) =$  \_\_\_\_\_.

(c) (3 Points) Let  $P(x)$  be a linear function perpendicular to  $L(x)$  and passing through the point  $(1, 0)$ . The equation of this linear function is  $P(x) =$  \_\_\_\_\_.

(Similar concepts to Practice Problems 8 and HW6 Questions 5-7)

- (2) A UAlbany student, Mariah, is selling custom-designed phone cases in the campus center to raise money for their club. The profit,  $P(n)$ , they make in dollars is modeled by the function:

$$P(n) = -0.5n^2 + 15n,$$

where  $n$  is the number of phone cases they sell in a day.

- (a) (4 Points) The number of phone cases Mariah needs to sell to maximize profit is \_\_\_\_\_ phone cases.

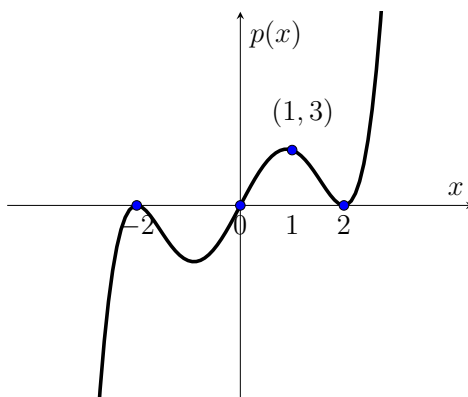
- (b) (4 Points) The maximum profit Mariah can make in a day is \_\_\_\_\_ dollars.

Problem 2 Continued

- (c) (**Optional Extra Credit Problem (4 Points)**) Determine the number of phone cases Mariah needs to sell to make a profit of exactly \$100.

(Similar concepts to Practice Problem 9 Question 3)

(3) (8 Points) Find a possible formula for the polynomial graphed below.



(Similar concepts to Practice Problems 10 Questions 1,2, Online HW 7 Questions 9, 10)

(4) The graph of  $y = f(x)$  has

- Vertical asymptotes at  $x = 3$  and  $x = 5$ .
- The  $x$ -intercept at  $(-5, 0)$  and  $(-4, 0)$ .
- A horizontal asymptote of  $y = \frac{1}{3}$ .

(6 Points) Find ONE possible formula for the rational function  $f$ .

(Similar to HW8 and Practice Problems 13)

- (5) (a) (3 Points) Find the domain of  $f(x) = \log(2 - 7x)$ . Write your answer using interval notation.

(b) (3 Points) The value of  $\ln\left(\frac{1}{e^7}\right) =$  \_\_\_\_\_.

(c) (3 Points) The value of  $100^{\log 5} =$  \_\_\_\_\_.

(Similar to HW8 Questions 5-9)

- (6) (a) (5 Points) Expand the expression below as a sum or difference of logarithms with no exponents.

$$\log\left(\frac{a^{-3}b^5}{c^{-7}}\right)$$

- (b) (5 Points) Solve for  $x$ :

$$3\log(2x + 6) = 6$$

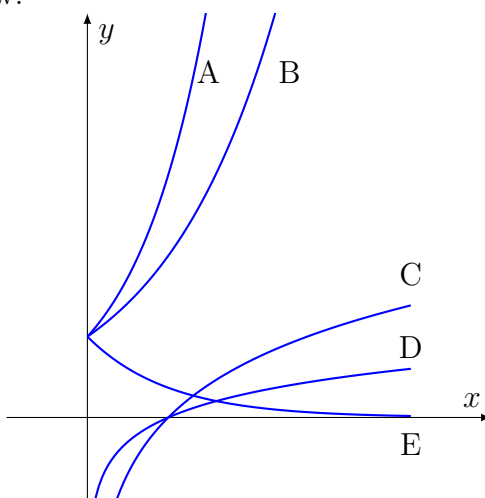


(7) (Similar to Practice Problems 13, HW8)

(a) (6 Points) Solve for  $x$ :

$$11 \cdot 3^x = 5 \cdot 7^x$$

(b) (**Optional Extra Credit Problem (4 Points)**) Match the functions with with their graphs in the figure below.



$y = 2^x$  is the graph labeled \_\_\_\_\_.

$y = e^{-x}$  is the graph labeled \_\_\_\_\_.

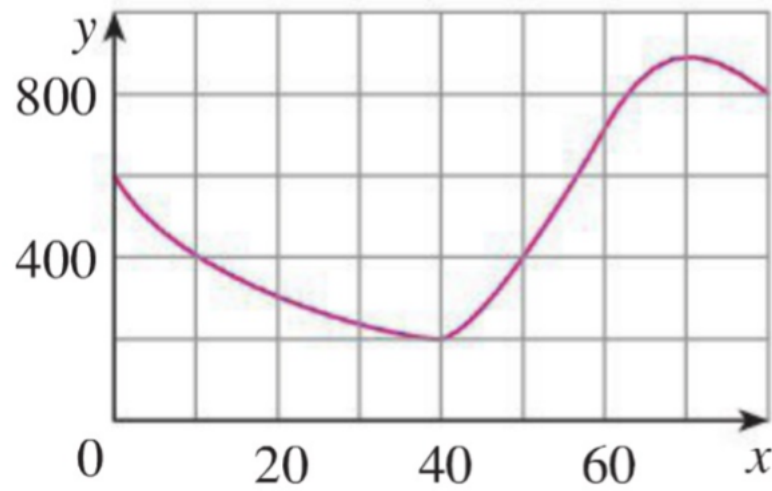
$y = 3^x$  is the graph labeled \_\_\_\_\_.

$y = \ln(x)$  is the graph labeled \_\_\_\_\_.

$y = \log(x)$  is the graph labeled \_\_\_\_\_.

**(Optional Extra Credit Problem: 4 Points)**

(8) Consider the graph of  $f(x)$  below.



Calculate the average rate of change of  $f(x)$  on the interval  $[10, 40]$ .